High–Angular–Momentum Structures in ^{64}Zn

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Abstract

High–angular–momentum states in ^{64}Zn were populated in the ^{40}Ca(^{28}Si,4p) reaction at a beam energy of 122 MeV. Evaporated, light, charged particles were identified by the Microball while gamma rays were detected using the Gammasphere array. The main focus of this paper is on two strongly coupled, collective bands. The yrast band, which was previously known, has been linked to lower–lying states establishing the excitation energies and angular momenta of in–band states for the first time. The newly identified excited band decays to the lower band but firm angular momentum assignments could not be made. In order to interpret these structures we have performed Cranked–Nilsson–Strutinsky calculations which have been extended to account for the distribution of nucleons within a configuration. We interpret the yrast collective band as based on the $\pi(f_{7/2})^{-1}(p_{3/2}f_{5/2})^2(g_{9/2})^1$ $\nu(p_{3/2}f_{5/2})^4(g_{9/2})^2$ configuration. There are several possible interpretations of the second band but it is difficult to distinguish between the different possibilities.

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I. INTRODUCTION

Recent observations of rotational bands in the proton–rich nuclei near $A \simeq 60$ are of considerable current interest [1–13]. The limited number of valence particles outside of the spherical doubly magic nucleus ^{56}Ni means that the low–angular–momentum decay schemes are dominated by spherical shell–model states. At higher angular momentum, collective bands dominate. Such bands provide an important testing ground for nuclear models enabling comparisons to be made between mean–field cranking models, traditionally used to describe collective behavior in heavier nuclei, and large–scale shell–model calculations.

The first rotational structure identified in this region was a strongly coupled band assigned to ^{64}Zn [2]. The characteristics of this band were very similar to those of smoothly terminating rotational bands in the Sn-Sb nuclei of the $A \simeq 110$ region [14]. Such terminating bands are expected in the $A \simeq 60$ region since the maximum angular momentum available from possible configurations is often limited to $I \simeq$20–30$\hbar$. Comparisons of the ^{64}Zn structure with Cranked–Nilsson–Strutinsky (CNS) calculations suggested a single–particle configuration involving a proton excitation across the $Z = 28$ spherical shell gap from the $f_{7/2}$ to the $g_{9/2}$ subshells, coupled with the excitation of two of the valence neutrons into the $g_{9/2}$ subshell. However, in the previous work of ref. [2] no transitions linking the band to lower–lying yrast states were observed and angular momentum and parity assignments were not possible. Motivated by the above considerations we performed an experiment to investigate collective structures in ^{64}Zn.

II. EXPERIMENTAL DETAILS

A. Analysis

High–angular–momentum states were populated in the ^{40}Ca(^{28}Si,4p) reaction at a beam energy of 122 MeV. The beam, accelerated by the ATLAS accelerator at the Argonne National Laboratory, was incident on a $\simeq$400μg/cm^2 ^{40}Ca foil with a flash of $\simeq$100μg/cm^2 Au

on both sides to prevent oxidation. Gamma rays were detected with the Gammasphere array [15] which, for this experiment, comprised 101 HPGe detectors. Light charged particles were detected with the Microball [16], a 4π array of 95 CsI(Tl) scintillators. Hevimet collimators were removed from the BGO suppressors to enable gamma–ray sum–energy and multiplicity measurements [17]. A total of 2.3×10^9 coincidence events, with at least four Compton–suppressed gamma rays, was collected. The ^{64}Zn residue was produced in approximately 15% of all fusion–evaporation events.

In the analysis, events associated with ^{64}Zn were selected by requiring the detection of four protons in the Microball (the detection efficiency for a single proton was measured to be 78%) in combination with a requirement that the total energy of the detected protons plus the total gamma–ray energy, measured in Gammasphere, was consistent with that expected for the 4p evaporation channel. This latter condition is an application of conservation of total energy and helps to reduce contaminants associated with other reaction channels when one or more of the evaporated particles goes undetected [18]. Over 95% of the fusion–evaporation events passing these requirements were associated with ^{64}Zn. Contaminant gamma rays that were positively identified came from the 4pn, 5p, and α3p channels and all had $\simeq$1% intensity relative to the 4p channel after the filters. The selected events were then sorted into various E_γ–E_γ coincidence matrices, and E_γ–E_γ–E_γ cubes. The analysis was performed using the RADWARE suite of programs [19].

During the off–line sorting, a correction to the mean recoil velocity according to the momentum vectors of the detected protons was applied to the gamma rays on an event–by–event basis [20]. A mean recoil velocity of v/c=0.0358 (where c is the speed of light) was used when investigating the low–angular–momentum states. This velocity is appropriate for nuclear states with lifetimes longer than the transit time in the target and was estimated from the mean Doppler shift of gamma–ray transitions which were emitted after the nucleus recoiled into vacuum. For high–angular–momentum states a mean recoil velocity of v/c=0.0397 was used and is more appropriate for states which have lifetimes that are much shorter than the transit time through the target. This corresponds to the calculated recoil

velocity for nuclei formed at mid–target and improves the energy resolution of gamma–rays emitted from states in collective bands. These two corrections are referred to as 'slow' and 'fast', respectively.

B. Results

1. The Level Scheme

The level scheme established by previous works [2,21–24] has been considerably modified and extended. The level scheme derived from our experiment is presented in Fig. 1. The main focus of this paper is on the two strongly coupled bands labelled A and B. As an illustration of the quality of the data, Fig. 2 shows a spectrum associated with a single coincidence gate on the 2689 keV ($23^{(-)} \to 21^{(-)}$) transition in band A. This strongly coupled band is the previously known collective band [2] and we estimate that it collects approximately 10% of the intensity of the $2^+ \to 0^+$, 991 keV ground–state transition. We have extended the topmost states by the addition of the 2814, 3571, and 3117 keV transitions. The 3461 keV transition was placed at the top of the band in the previous work [2] and has been reassigned as a transition decaying from near the bottom of the band. The band has also been extended towards lower angular momentum by the addition of the 1020 keV ($13^{(-)} \to 11^{(-)}$) transition. The structure has been firmly linked to low–lying states. Fig. 3 shows the high energy portion of the spectrum derived from a single gate of the 603 keV ($15^{(-)} \to 14^{(-)}$) in–band dipole transition in the 'slow' matrix. Several of the linking transitions can be clearly seen.

Band B is a newly observed structure with an intensity $\simeq 1\%$ relative to the $2^+ \to 0^+$ 991 keV transition. Fig. 4 shows a coincidence spectrum associated with a single gate on the 2429 keV transition in band B. It is clear from Fig. 4 that the 2429 keV transition is in coincidence with transitions of band A indicating that there is some connection between the two structures. Indeed, as shown in the level scheme of Fig. 1, we have identified a number of transitions (561, 742, 769 keV) which decay from the upper states of band B to

lower states in band A. Each of these interband transitions carries approximately 30% of the total observed decay intensity from their respective initial states. To illustrate the interband decays, Fig. 5 presents a spectrum generated by requiring a double coincidence between the 563 keV dipole transition in band A with the 2429 keV quadrupole transition of band B. The 561 keV inter–band transition is clearly visible as are the expected coincidences with other members of band A. If we require a double coincidence between the 563 keV dipole transition in band A with the 2099 keV quadrupole transition of band B no connection is present (see Fig. 5). Such coincidence relationships helped us identify the inter–band decay pathways shown in Fig 1. We have also tentatively placed a 1792 keV gamma ray which depopulates the lowest observed in–band state into a lower–lying state.

2. Angular Momentum Asssignments

To determine the angular momenta of states, directional correlation ratios from oriented nuclei (DCO ratios) were analyzed. Such a DCO ratio was defined by the intensity, corrected for detection efficiency, of a given pair of coincident transitions in the two E_γ–E_γ matrices corresponding to $\pm35°/\pm35°$ and $\pm80°/\pm80°$, where $\pm35°$ was formed from summing the subset of detectors with angles (relative to the beam axis) $\theta=\pm31.7°$ and $\pm37.4°$, and $\pm80°$ from the subset with $\theta=\pm79.2°$ and $\pm80.7°$. Thus, the DCO ratio is defined as:

$$R_{DCO} = \frac{\mathcal{I}_{\gamma\gamma}(\pm35, \pm35)}{\mathcal{I}_{\gamma\gamma}(\pm80, \pm80)} \tag{1}$$

Coincident pairs of known stretched E2 transitions provided a measure of the nuclear spin alignment given by the dimensionless parameter σ/I where, for an initial state of angular momentum I, it is assumed that there is a Gaussian distribution of m–substates centered at m=0 with standard deviation σ. For such transitions we found R_{DCO}=1.74(10) corresponding to σ/I=0.32(4) at I=17 (see Fig. 6a.). Using this value of σ/I allowed us to estimate the expected R_{DCO} values for common correlations ($I{\rightarrow}I{-}1{\rightarrow}I{-}2$, $I{\rightarrow}I{-}1{\rightarrow}I{-}3$, etc.) and to assign the I values shown in Fig. 1.

Additional information on the angular momentum assignments was obtained by measuring γ–ray anisotropies, or angular distribution ratios. Such a ratio was defined by the intensity, corrected for detector efficiency, of a transition detected at $\pm35°$ over the intensity when detected at $\pm80°$. Clean spectra were obtained by requiring a coincidence with another transition detected in any other detector, regardless of angle. By summing over all the detector angles of Gammasphere an essentially spherical average over the gating transition was taken yielding an angular distribution (rather than a DCO) ratio.

As an example of this analysis Table I gives the measured intensities, DCO ratios (R_{DCO}), angular distribution ratios (R_{AD}), and the angular momentum assignments determined for transitions using a single gate on the 710 keV ($16^{(-)} \rightarrow 15^{(-)}$) transition in band A. We note that the average R_{DCO} value for the dipoles in band A is R_{DCO}=0.80(2) and the average for the in–band strecthed quadrupoles is R_{DCO}=1.34(6). These correlation ratios are consistent with an E2/M1 mixing ratio, δ, for the in–band stretched–dipole transitions of $\delta \approx$0.05 (using the same phase convention as that used in [25]) – see Fig. 6b). This mixing ratio would correspond to a value of the angular distribution of R_{AD}=0.86 for a value of σ/I=0.3. The measured average of the dipoles in band A presented in Table I is R_{AD}=0.79(2). Using the 710 keV dipole as a gate and assuming σ/I=0.3, we expect a value of $R_{AD} \approx$1.41 for stretched quadrupole transitions. Assuming that all the low–lying stretched quadrupole transitions are electric quadrupoles, it follows that states in band A are likely negative parity.

As mentioned above, band B is much weaker than band A. Angular distribution measurements were sufficient to show the dipole character of the crossover transitions and the quadrupole character of the presumed E2 transitions. However, reliable R_{DCO} or R_{AD} ratios could not be extracted for the transitions connecting band B to band A. Therefore, we do not have firm angular momentum assignments for the states in band B. The intensity of band A is around 10 times greater than the intensity of band B suggesting that it is the more yrast of the two structures in the region where they are fed. This suggests that the interband trasitions may be $I \rightarrow I$ transitions as indicated in Fig. 1.

We have determined that the $\Delta I=1$ crossover transitions in band A are relatively pure stretched dipoles, presumably magnetic dipoles as expected for decays between strongly coupled partner bands. It seems reasonable to assume that this is also the case for transitions in band B. We can then determine the B(M1)/B(E2) ratios, which may help in assigning nucleon configurations to the bands. The expression used to determine these ratios is:

$$\frac{B(M1)}{B(E2)} = 0.697 \frac{E_\gamma(I \to I-2)^5}{E_\gamma(I \to I-1)^3} \frac{1}{\lambda} \frac{1}{(1+\delta^2)} \qquad [(\mu_N/eb)^2] \qquad (2)$$

where, E_γ is given in MeV and λ is the branching ratio expressed as:

$$\lambda = \frac{\mathcal{I}_\gamma(I \to I-2)}{\mathcal{I}_\gamma(I \to I-1)} \qquad (3)$$

The branching ratios were determined by setting a single gate on a transition decaying into the state of interest and measuring the intensities of the gamma rays depopulating that state. The small effect of the mixing ratio, δ, was ignored. The resulting B(M1)/B(E2) ratios for bands A and B are given in table II. The values for bands A and B agree within errors and are roughly constant for all measured values.

III. THEORETICAL INTERPRETATION

A. General Considerations

The nucleus ^{64}Zn has two protons and six neutrons outside the spherical doubly magic core of ^{56}Ni ($N = Z = 28$). Low–lying valence configurations involve active orbitals from the $\mathcal{N} = 3$ $p_{3/2}$ and $f_{5/2}$ subshells and the $\mathcal{N} = 4$ $g_{9/2}$ intruder subshell. Higher angular momentum states can be formed by exciting one or more protons from the $\mathcal{N} = 3$ $f_{7/2}$ subshell across the $Z = 28$ shell gap, giving rise to deformed, collective, band structures as observed in several nuclei of this mass region [1–13].

In an effort to assign configurations to the observed structures in ^{64}Zn, we have carried out configuration-dependent Cranked–Nilsson-Strutinsky (CNS) calculations. We follow the

formalism described in references [14,26]. Pairing is neglected in these calculations so they can only be used to get a qualitative understanding of the states with low angular momentum but they should become realistic for higher values, say $I > 10\hbar$, in this mass region. Configurations will be labelled as $[p_1p_2, n_1n_2]$ defining the occupation of the active subshells,

$$\pi\left(f_{7/2}\right)^{-p_1}\left(p_{3/2}f_{5/2}\right)^{2+p_1-p_2}\left(g_{9/2}\right)^{p_2}\nu\left(f_{7/2}\right)^{-n_1}\left(p_{3/2}f_{5/2}\right)^{6+n_1-n_2}\left(g_{9/2}\right)^{n_2}$$

That is, p_1 (n_1) is the number of proton (neutron) holes in the $f_{7/2}$ subshell and p_2 (n_2) is the number of protons (neutrons) in the $g_{9/2}$ subshell. Similar calculations have previously been carried out for ^{64}Zn [2] and for several other nuclei in this region, including ^{59}Cu [11], ^{62}Zn [1,3] and ^{68}Ge [9]. In general, for a nucleus with only a few particles (and holes) outside the $Z = N = 28$ core, the configurations are rather pure and easy to interpret. With more particles outside the core, as in the case of ^{68}Ge [9], the situation becomes more complex.

It is useful at this stage to make a few remarks on terminology and to broadly outline the main points in the sections to come. We use the word configuration to refer to the occupation of active subshells as discussed in the previous paragraph. As we shall see in subsection III B, standard CNS calculations do not take into account the specific distribution of the nucleons within that configuration. In other words, different states can be formed by the redistribution of nucleons within specific subshells belonging to the same 'fixed' configuration. In order to trace these states, we must go beyond the standard CNS formalism. The extended CNS calculations, and the resulting interpretation of band A, are presented in subsection III C. Possible interpretations of band B are discussed in subsection III D.

B. Standard CNS Calculations

First, we make a general overview of the calculated structures in ^{64}Zn. Using standard parameters [26], we have searched for the yrast states and other low–lying configurations for different combinations of parity and signature. These states are shown relative to a standard rotating reference [14] in Fig. 7. The highest angular momentum which can be

built in the valence space of $(p_{3/2}f_{5/2})$ protons and neutrons is $I = 10$. However, this 10^+ state is calculated to have a relatively high excitation energy. The lowest calculated states for $I = 10 - 15$ involve one, two, or even three $g_{9/2}$ particles. These configurations often terminate in low-lying non-collective aligned states at a large oblate deformation. Generally, the $(p_{3/2}f_{5/2})$ particles involved in the configurations of these states do not contribute their maximum angular momentum. This can be seen in table III where the contribution from the different subshells is given for some of these low-lying states. At higher angular momentum, it becomes favorable to promote one proton from the $f_{7/2}$ subshell across the $Z = 28$ gap. These configurations are drawn with thick shaded lines in Fig. 7. They correspond to the first bands which appear to show 'real' collectivity. For even higher values of the angular momentum, it becomes favorable to create more holes (particles) in the $f_{7/2}$ ($g_{9/2}$) subshells leading to larger deformations and enhanced collectivity.

To compare experiment with calculation, band A is of main interest since band B does not have firm I^π assignments. Band A, was assigned to the [11,02] configuration in reference [2]. Now that it has been connected to the low-angular-momentum states and observed to the $I^\pi = 26^{(-)}$ state (see Fig. 1), it seems that this assignment is confirmed. There are two calculated [11,02] configurations which are relatively low in energy (see Fig. 7). These two configurations differ in the distribution of the four neutrons in the $(p_{3/2}f_{5/2})$ orbitals. The configuration which is lowest for most angular momentum values has two neutrons in each of the $\alpha = \pm 1/2$ orbitals, while the other configuration has three neutrons in $\alpha = 1/2$ and one in $\alpha = -1/2$. For the terminating states of this latter configuration (listed in table III, $I = 22, 23$) these four $(p_{3/2}f_{5/2})$ neutrons couple to $I = 3$. However, the corresponding band is calculated to be very irregular and lie low in energy for only a few angular–momentum values, especially $I = 22$. Therefore, it is only the more regular [11,02] band which is relevant for the interpretation of band A.

The calculated $\alpha = 1$ states (odd-I values) behave regularly only up to $I^\pi = 23^-$ which is predicted to be a non-collective state with $\gamma = 60°$. This aligned 23^- state terminates the lowest [11,02] band. The aligned 25^- state, connected to this 23^- state in Fig. 7,

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corresponds to the terminating state of a different excited sequence. As seen in table III, the difference between these two aligned states is that the four neutrons in the $(p_{3/2}f_{5/2})$ orbitals contribute either $4\hbar$ or $6\hbar$ of angular momentum, respectively. The calculated termination at $I^{\pi} = 23^-$ disagrees with the observed odd–I sequence which behaves regularly all the way up to and including the $I^{\pi} = 25^-$ state. In contrast, the $\alpha = 0$ states (even-I values) behave regularly all the way up to the $I^{\pi} = 26^-$ state in agreement with experiment. It is surprising that the calculated odd–I and even–I states display this different behavior as they approach termination since they only differ by the signature the $f_{7/2}$ hole (see table III). It is probable that this discrepancy can be removed by making small changes to the single–particle parameters used in the calculation (see below).

The shape trajectories for the two lowest [11,02] configurations are shown in Fig. 8. Consider first the yrast, odd-angular–momentum states for which the shape changes smoothly from $\varepsilon_2 \approx 0.31$, $\gamma \approx 20°$ at $I^{\pi} = 11^-$ to the terminating $I^{\pi} = 23^-$ state at $\varepsilon_2 \approx 0.28$, $\gamma = 60°$. This contrasts with the shape trajectory for the even–I states which follows the odd–I trajectory up to $I \approx 20$ but then moves toward decreasing ε_2-values (with approximately a constant value of γ) before reaching a non-collective $\gamma = 60°$ $I^{\pi} = 26^-$ state. The deformation of this $I = 26$ state is considerably smaller ($\varepsilon_2 = 0.22$) than that of the $I = 23$ state ($\varepsilon_2 = 0.28$). The S-shape of the even–I trajectory suggests some kind of band-crossing at $I \approx 22\hbar$.

The single–particle orbitals along the odd–I shape–trajectory are drawn in Fig. 9 where, at each deformation, the rotational frequency has been fitted to give the appropriate angular–momentum value. For the protons, there is a big gap at $Z = 31$ and the odd–I states are formed by creating one hole in the highest $f_{7/2}$ orbital (labelled 3_5) below this gap, while the even–I states require the hole to be in the signature–partner orbital. These orbitals, which are drawn with thick shaded lines in Fig. 9, are essentially degenerate at low–angular–momentum but separate in energy at higher angular–momentum. The neutron orbitals are filled up to the $N = 34$ gap. At $\gamma = 60°$ there is an orbital just below the gap, labelled 3_6, which has an aligned angular momentum of $m_i = -0.5\hbar$. At this same point in the

shape trajectory, there is another orbital at slightly higher energy, labelled 3_7, which has the same signature and parity but an aligned angular momentum of $m_i = 1.5$. These differences in the m_i-values imply that if the 34th particle is raised to the higher–lying 3_7 orbital, an excited configuration exists which will terminate $2\hbar$ higher than the yrast sequence. That is, the excited configuration will terminate at $I = 25$. The even–I states appear to behave differently, terminating at $I^{\pi} = 26^-$ and not at $I^{\pi} = 24^-$. This suggests that, for the corresponding shape trajectory, the ordering of these two neutron orbitals (3_6 and 3_7) is already reversed at $\gamma = 60°$. Therefore, they must interact before reaching the non-collective limit at $\gamma = 60°$ which is consistent with the band-crossing scenario discussed above. The two configurations which interact will have the same labelling within our scheme. In order to study such a situation in detail we must extend the standard CNS formalism to include a way to follow such structures which may be regarded as excitations within a 'fixed' configuration.

C. Extended CNS Calculations

In principle, it should be straightforward to calculate not only the yrast states but also excited states associated with fixed configurations. However, without additional constraints, the first excited state might correspond to a different excitation at each angular–momentum value. To overcome this problem it is possible to define in which group of orbitals an excitation is allowed (for example, in the low-j $\mathcal{N} = 3$ orbitals with $\alpha = -1/2$). The difficulty is then to define the excited state in the full space of deformation and rotational frequency. In general, this is not possible because of different virtual crossings between orbitals with identical quantum numbers. For example, an excited state could correspond to either a single-particle excitation at a constant deformation or to a state in a secondary minimum at a different deformation. However, by limiting the changes in deformation and rotational frequency, it is often possible to define a unique yrast sequence and to specify which excitation is allowed with respect to these yrast states. In order to provide a full interpretation of band A and to search for possible explainations of band B, the CNS formalism as described

in reference [14] was generalized to calculate and identify excitations of this kind.

Considering the orbitals in Fig. 9, the lowest states of the [11,02] type are well defined. Starting from these states, we have calculated the next highest excited states, specifying excitations within the low-j, $\mathcal{N} = 3$, $\alpha = -1/2$ neutron orbitals. This corresponds to a neutron being excited from the lower (3_6) to the upper (3_7) thick shaded orbital in the lower panel of Fig. 9. For odd–I excited states, we obtain a smooth, well-defined deformation trajectory which can be followed up to $I^\pi = 25^-$ (see Fig. 8). This state is non-collective with $\varepsilon_2 \approx 0.25$, $\gamma = 60°$ and was connected smoothly to the aligned yrast $I^\pi = 23^-$ state in Fig. 7. For the even–I states, the yrast band can be followed to the $I^\pi = 26^-$ state as discussed above.

There seems to be a clear tendency for the highest angular momentum states to be calculated at a higher excitation energy relative to the observed energies. For ^{64}Zn with only a few particles in the ($p_{3/2}f_{5/2}$) subshells, the highest angular–momentum states will become more favored if the high-j subshells are made to have lower energy in the calculation (that is, the $f_{5/2}$ subshell is lowered relative to the $p_{3/2}$ subshell). The parameters recently used to describe the decay out of the superdeformed band in ^{59}Cu [27] indicate that such small changes are reasonable. In that case, the $f_{5/2}$ subshell was found to be approximately 300 keV closer to the $p_{3/2}$ subshell (corresponding to $0.025\hbar\omega_0$ closer in oscillator units as used in Fig. 9). We have performed new calculations for the configurations in ^{64}Zn using these revised parameters. The new calculations for the yrast [11,02] sequences are compared with band A in Fig. 10. The agreement with experiment is almost perfect all the way from the lowest $I^\pi = 11^-, 12^-$ states to the terminating $I^\pi = 25^-, 26^-$ states. The calculated shape trajectory for the even–I states is very similar to that already shown in Fig. 8. The odd–I states now follow a trajectory close to that of the even–I states with a similar S–shape and terminating at $\varepsilon_2 \approx 0.25$, $\gamma = 60°$.

Shown in Fig. 11 are the calculated single-neutron orbitals using the revised parameters. The calculation was performed at a fixed deformation close to the predicted shape associated with the yrast and excited [11,02] bands at $I = 21, 22$. It is evident that the 6th and 7th

$\alpha = -1/2$, $\mathcal{N} = 3$ orbitals come close to each other, interchanging character at $\omega = 0.12\omega_0$, and passing through a virtual crossing. This is the approximate frequency at which the $I = 21, 22$ states are expected. This crossing is not clearly visible in the behavior of calculated energies drawn in Fig. 10, indicating a large interaction strength. However, this interaction will influence the curvature of the calculated sequences in Fig. 10 and, since there is excellent agreement with experiment, this crossing is important for a detailed understanding of band A.

D. Possible interpretations of band B

It is interesting to see if an interpretation can be found for band B, assuming that the suggested angular momentum assignments in Fig. 1 are correct. The B(M1)/B(E2) ratios measured for bands A and B are identical within errors (see Table II) supporting the suggestion that the two bands are based on similar configurations involving only one $f_{7/2}$ proton hole. This is also consistent with the range of angular momentum over which the band is seen.

There are several possible interpretations of band B. The band might correspond to the second [11,02] configuration (drawn in Fig. 7) which terminates in aligned states with $I^\pi = 22^-$ and $I^\pi = 23^-$, which is consistent with the suggested angular momentum assignments. However, the calculation for this configuration fails to reproduce several features of the observed band B including its excitation energy relative to band A. It is not drawn in the lower panel of Fig. 10.

Another possibility is that band B could be an excitation of the yrast [11,02] configuration as discussed in the previous subsection. The band resulting from such a calculation terminates at $I^\pi = 23^-$ and $I = 24^-$. The prediction for the two signatures is drawn in the lower panel of Fig. 10. The calculated energies at the highest angular momenta are in general agreement with experiment but the discrepancy gets worse for lower I values.

As drawn in Fig. 1, band B is clearly less yrast than band A at high angular momentum

(which is also reasonable from the point of view of the relative population of the two bands). It would then seem reasonable to expect that the underlying configuration of band B involves fewer $g_{9/2}$ particles. Possible configurations of this kind are are [11,01] (with one $g_{9/2}$ proton and one $g_{9/2}$ neutron) or [10,02] (no $g_{9/2}$ protons and two $g_{9/2}$ neutrons). The calculated sequences based on these configurations are drawn in the lower panel of Fig. 10. They both have positive parity and terminate at $I^\pi = 23^+$ in agreement with the observed maximum angular momentum of band B.

The [11,01] sequences are also drawn if Fig. 7, where the two signatures were seen to behave in a rather irregular way. This discrepancy with experiment may be due to the details of the potential energy surface associated with this configuration which involves a more collective minimum at slightly higher excitation energy. This would result in smoother behavior for the two signatures and the resultant sequences are drawn in Fig. 10. It is difficult to explain why band B should be associated with the collective minimum rather than the lower-energy irregular states of this configuration but this could be an interpretation of the band.

The [10,02] configuration appears to be too high in excitation energy to be a reasonable alternative (see Fig. 10). The high excitation energy is due to the large signature splitting between the two lowest $g_{9/2}$ neutron levels which makes it energetically unfavorable to have two neutrons occupying these orbitals.

IV. SUMMARY

In summary, high–angular–momentum states in ^{64}Zn were investigated in an experiment using Gammasphere and the Microball. The level scheme was considerably revised and extended. The main focus of this paper has been on two strongly coupled bands. One of these bands was known from a previous study. This structure has been firmly linked to low–lying states, establishing the excitation energies, angular momenta, and probable parity of the in–band states. An excited band is seen to decay to the lower–lying band and

several interband transitions have been identified. The angular momenta and parity of the states in this second band could not be firmly established. These structures are important examples of the onset of collective rotational behavior in the limited valence space outside the $N = Z = 28$ spherical shell gaps.

In order to interpret the bands, the standard Cranked–Nilsson–Strutinsky formalism was extended to allow yrast and excited states to be calculated within fixed configurations and to find their self–consistent deformations. The lowest collective band in ^{64}Zn is interpreted as based on the $\pi(f_{7/2})^{-1}(p_{3/2}f_{5/2})^2(g_{9/2})^1 \ \nu(p_{3/2}f_{5/2})^4(g_{9/2})^2$ configuration (labelled [11,02] in our notation) and our calculations reproduce the observed in–band states to an excellent accuracy. The second band has several alternative interpretations, but on the basis of the current work we are unable to distinguish between them. One aspect that may provide an important clue is the interband decay from this excited structure to the lower band.

TABLES

TABLE I. Measured transition energies, intensities, DCO ratios (R_{DCO}), angular distribution ratios (R_{AD}), and angular–momentum assignments for transitions in ^{64}Zn measured from a single coincidence gate on the 710 keV stretched–dipole transition in band A. The intensities were corrected for detection efficiency and are given as a percentage of the 991 keV $2^+ \rightarrow 0^+$ transition. The numbers above the solid dividing line are in–band states of band A while those below it are from lower–lying states.

E_γ (keV)	Intensity	R_{DCO}	R_{AD}	$I_i^\pi \rightarrow I_f^\pi$
508.1(5)	–	–	–	$12^{(-)} \rightarrow 11^{(-)}$
512.0(5)	–	–	–	$13^{(-)} \rightarrow 12^{(-)}$
563.3(3)	65.5(3)	0.78(2)	0.76(2)	$14^{(-)} \rightarrow 13^{(-)}$
603.0(3)	102.7(4)	0.79(2)	0.81(2)	$15^{(-)} \rightarrow 14^{(-)}$
709.5(3)	–	–	–	$16^{(-)} \rightarrow 15^{(-)}$
746.4(3)	87.2(4)	0.86(2)	0.81(3)	$17^{(-)} \rightarrow 16^{(-)}$
865.8(5)	25.8(3)	0.78(3)	0.86(8)	$18^{(-)} \rightarrow 17^{(-)}$
914.5(5)	29.6(3)	0.80(5)	0.83(5)	$19^{(-)} \rightarrow 18^{(-)}$
1082.1(5)	13.7(3)	–	–	$20^{(-)} \rightarrow 19^{(-)}$
1142.0(5)	4.1(8)	–	–	$21^{(-)} \rightarrow 20^{(-)}$
1395.6(9)	4.2(2)	–	–	$22^{(-)} \rightarrow 21^{(-)}$
1292(1)	–	–	–	$23^{(-)} \rightarrow 22^{(-)}$
1523(1)	–	–	–	$24^{(-)} \rightarrow 23^{(-)}$
1020.0(5)	6.0(2)	–	–	$13^{(-)} \rightarrow 11^{(-)}$
1074.7(5)	15.9(4)	–	–	$14^{(-)} \rightarrow 12^{(-)}$
1166[1]	52.4(4)	1.27(11)	1.25(6)	$15^{(-)} \rightarrow 13^{(-)}$
1312.5(9)	–	–	–	$16^{(-)} \rightarrow 14^{(-)}$

[1]contaminated

18

1455.2(5)	–	–	–	$17^{(-)} \to 15^{(-)}$
1613.3(6)	57.4(11)	–	1.09(8)	$18^{(-)} \to 16^{(-)}$
1779.6(6)	30.5(3)	1.31(6)	1.24(9)	$19^{(-)} \to 17^{(-)}$
1997.4(6)	29.9(4)	1.44(9)	1.16(8)	$20^{(-)} \to 18^{(-)}$
2225.1(10)	22.0(4)	1.27(11)	1.35(12)	$21^{(-)} \to 19^{(-)}$
2538.6(10)	14.8(3)	1.26(15)	1.23(16)	$22^{(-)} \to 20^{(-)}$
2688.5(10)	11.2(6)	1.47(27)	1.15(6)	$23^{(-)} \to 21^{(-)}$
2814(1)	4.5(2)	–	–	$24^{(-)} \to 22^{(-)}$
3117(1)	1.1(1)	–	–	$25^{(-)} \to 23^{(-)}$
3571(1)	–	–	–	$26^{(-)} \to 24^{(-)}$
398.2(3)	9.5(2)	0.61(5)	0.69(6)	$7^- \to 6^+$
429.8(3)	1.2(1)	–	1.24(44)	$4^+ \to 4^+$
547.4(3)	2.0(1)	–	0.87(15)	$8^{(-)} \to 7^{(-)}$
584.8(5)	3.8(2)	–	0.80(8)	$12^{(-)} \to 11^{(-)}$
592.5(3)	9.4(2)	0.58(8)	0.68(8)	$6^{(-)} \to 6^{(+)}$
617.9(5)	1.7(1)	–	–	$5^- \to 4^{(+)}$
641.4(5)	47.0(3)	0.73(2)	0.80(3)	$7^- \to 6^+$
656.7(5)	3.0(1)	–	1.28(24)	$13^{(-)} \to 11^{(-)}$
771.2(5)	2.9(1)	0.56(15)	0.80(18)	$4^{(+)} \to 4^+$
808.4(5)	12.4(3)	0.81(6)	0.71(6)	$2^+ \to 2^+$
824.6(5)	3.7(2)	–	1.66(13)	$7^{(-)} \to 5^{(-)}$
926.2(5)	4.9(2)	–	1.43(11)	$5^- \to 3^-$
936.7(5)	15.6(3)	1.25(7)	1.17(9)	$4^+ \to 2^+$
955.0(5)	6.1(2)	1.04(15)	1.34(17)	$8^{(-)} \to 6^{(-)}$
971.1(5)	5.3(2)	–	1.62(40)	$9^{(-)} \to 7^{(-)}$
991.0(5)	100.0(19)	1.19(3)	1.17(2)	$2^+ \to 0^+$

$999.9(6)^2$	4.8(4)	–	0.92(3)	$6^{(+)} \to 4^{(+)}/4^{(+)} \to 4^+$
1029.9(5)	3.3(2)	–	1.31(10)	$8^{(-)} \to 6^{(-)}$
1046.2(5)	19.2(3)	1.34(15)	1.44(18)	$11^{(-)} \to 9^{(-)}$
1056.4(5)	17.6(3)	1.27(17)	1.70(15)	$7^{(-)} \to 5^-$
1064.1(5)	4.3(2)	–	–	$8^{(-)} \to 7^-$
1144.4(4)	15.3(41)	0.90(24)	1.01(7)	$8^{(+)} \to 7^-$
1227.2(6)	1.3(1)	–	1.39(9)	$7^{(-)} \to 5^-$
1260.3(7)	15.6(2)	1.21(12)	1.15(11)	$11^{(-)} \to 9^{(-)}$
1304.9(5)	5.8(2)	–	–	$12^{(-)} \to 11^{(-)}$
1315^3	113.4(5)	1.12(4)	1.39(3)	$4^+ \to 2^+/9^{(-)} \to 7^-$
1340.0(7)	12.4(2)	1.26(15)	1.26(11)	$6^{(+)} \to 4^+$
1363.0(4)	6.9(2)	1.46(32)	1.33(31)	$10^{(-)} \to 8^{(-)}$
1397.0(5)	4.3(2)	–	–	$8^{(+)} \to 7^-$
1500.3(5)	9.2(2)	1.74(20)	1.64(24)	$6^+ \to 4^+$
1618.6(5)	20.4(5)	–	–	$5^- \to 4^+$
1622.5(8)	0.8(5)	–	–	$11^{(-)} \to 10^{(-)}$
1686.9(5)	45.5(4)	1.27(17)	1.36(5)	$6^+ \to 4^+$
1773.2(10)	2.8(5)	–	–	$6^{(+)} \to 4^+$
1799.6(7)	5.5(2)	–	1.56(33)	$2^+ \to 0^+$
1850.4(10)	2.3(4)	–	–	$5^{(-)} \to 4^+$
1935.3(7)	4.1(3)	1.61(28)	1.46(10)	$6^+ \to 4^+$
2005.0(10)	2.4(3)	–	–	$3^- \to 2^+$
2037.8(7)	5.8(3)	1.66(22)	1.37(18)	$8^{(+)} \to 6^+$
2086.2(7)	5.6(2)	–	1.12(43)	$4^{(+)} \to 2^+$

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[2]multiple unresolved transitions

[3]mutiple unresolved transitions

2129.7(7)	2.6(2)	–	1.49(9)	$8^{(+)} \to 6^+$
2158.3(9)	4.3(2)	–	–	$13^{(-)} \to 12^{(-)}$
2321.9(9)	3.6(2)	–	–	$11^{(-)} \to 10^{(+)}$
2720(1)	1.1(1)	–	–	$14^{(-)} \to 12^{(-)}$
2886(1)	1.1(1)	–	1.52(30)	$12^{(-)} \to 10^{(-)}$
2950(1)	4.4(2)	0.87(8)	0.91(8)	$12^{(-)} \to 11^{(-)}$
3247(1)	2.9(1)	–	1.24(10)	$13^{(-)} \to 11^{(-)}$
3461(1)	5.5(2)	1.37(29)	1.69(51)	$13^{(-)} \to 11^{(-)}$

TABLE II. Measured B(M1)/B(E2) ratios for bands A and B (above and below the solid dividing line, respectively).

$E_\gamma(\Delta I{=}1)$	$E_\gamma(\Delta I{=}2)$	$B(M1)/B(E2)(\mu_N/eb)^2$
563	1075	15.3(10)
603	1166	12.8(9)
710	1313	–
746	1455	12.3(18)
866	1613	10.6(5)
915	1780	12.6(11)
1082	1997	15.3(10)
1142	2225	14.5(12)
1396	2539	15.2(12)
1292	2689	12.7(18)
856	1860	9.9(21)
1067	1924	12.1(20)
1032	2099	14.0(40)

TABLE III. Low-lying calculated terminating states in ^{64}Zn. The $(\varepsilon_2, \varepsilon_4)$ deformation at termination ($\gamma = 60°$) is given in the third column. The angular momentum contribution from different groups of orbitals ($(pf) \equiv (p_{3/2}f_{5/2})$) is shown as a subscript in the fourth column.

I	$[p_1p_2, n_1n_2]$	Deformation, $(\varepsilon_2, \varepsilon_4)$	Configuration
13^+	$[01,01]$	$(0.24, -0.014)$	$\pi(pf)^1_{1.5,2.5} (g_{9/2})^1_{4.5}$
14^+	$[01,01]$	$(0.26, -0.018)$	$\nu(pf)^5_{2.5} (g_{9/2})^1_{4.5}$
18^+	$[11,01]$	$(0.24, -0.014)$	$\pi(f_{7/2})^{-1}_{2.5}(pf)^2_4 (g_{9/2})^1_{4.5}$
			$\nu(pf)^5_{2.5} (g_{9/2})^1_{4.5}$
11^-	$[00,01]$	$(0.18, 0.005)$	$\pi(pf)^2_4$
			$\nu(pf)^5_{2.5} (g_{9/2})^1_{4.5}$
17^-		$(0.26, 0.005)$	
18^-	$[01,02]$	$(0.28, 0.000)$	$\pi(pf)^1_{1.5,2.5} (g_{9/2})^1_{4.5}$
18^-		$(0.27, -0.008)$	$\nu(pf)^4_{3,4} (g_{9/2})^2_8$
19^-		$(0.30, -0.015)$	
23^-		$(0.28, -0.013)$	
25^-	$[11,02]$	$(0.25, -0.004)$	$\pi(f_{7/2})^{-1}_{2.5,3.5}(pf)^2_4 (g_{9/2})^1_{4.5}$
26^-		$(0.22, 0.010)$	$\nu(pf)^4_{4,6} (g_{9/2})^2_8$
22^-	$[11,02]$	$(0.27, -0.002)$	$\pi(f_{7/2})^{-1}_{2.5,3.5}(pf)^2_4 (g_{9/2})^1_{4.5}$
23^-		$(0.25, 0.010)$	$\nu(pf)^4_3 (g_{9/2})^2_8$

ACKNOWLEDGMENTS

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FIGURES

FIG. 1. Level scheme for ^{64}Zn from the present experiment. The widths of the arrows are proportional to the measured gamma–ray intensity.

FIG. 2. Low and high energy portions (top and bottom, respectively) of a coincidence spectrum obtained from the 'fast' matrix by requiring a single gate on the 2689 keV quadrupole transition of band A. In–band transitions are labelled 'A'.

FIG. 3. Coincidence spectrum obtained from the 'slow' matrix by requiring a single gate on the 603 keV dipole transition of band A. The transitions linking the band to lower lying states are labelled 'L' while in–band gamma rays are labelled 'A'

FIG. 4. Low and high energy portions (top and bottom, respectively) of a coincidence spectrum obtained from the 'fast' matrix by requiring a single gate on the 2429 keV quadrupole transition of band B. In–band transitions are labelled 'B', transitions in band A are labelled 'A', and coincident transitions not yet placed in the level scheme are labelled '?'.

FIG. 5. a)Spectrum obtained by requiring a double coincidence between the 563 keV dipole transition of band A with the 2429 keV quadrupole transition of band B. b) Spectrum obtained by requiring a double coincidence between the 563 keV dipole transition of band A with the 2099 keV quadrupole transition of band B.

FIG. 6. a) The solid curve is the calculated variation of R_{DCO} for a stretched–quadrupole $\leftrightarrow$ stretched–quadrupole correlation as a function of the nuclear spin alignment parameter, σ/I (see text). The open point is the experimental average value. The vertical errors indicate the experimental uncertainty of this quantity while the horizontal errors give the corresponding uncertainty in σ/I. b) Plots of R_{DCO} for a stretched–dipole$\leftrightarrow$stretched–dipole correlation as a function of arctan(δ) where δ is the E2/M1 mixing ratio. The horizontal solid line is the average experimental value for in-band ΔI=1 transitions. The other solid curve are the values calculated assuming σ/I=0.32. Dashed lines and curves are the uncertainties.

FIG. 7. The calculated low-lying rotational bands of ^{64}Zn drawn relative to a rigid–rotor reference. Each panel corresponds to fixed parity, π, and signature exponent, α. The configurations with one proton hole in the f$_{7/2}$ subshell are drawn with thick shaded lines. Aligned states at, or very close to, $\gamma = 60°$ are circled.

FIG. 8. Calculated deformations for the [11,02] configurations in ^{64}Zn using standard parameters [26]. The yrast states are shown by large circles and the states with one excited $\alpha = -1/2$ low-j, $\mathcal{N} = 3$ neutron by smaller circles.

FIG. 9. Single-particle orbitals along the path, calculated with standard parameters as in Fig. 8, of the lowest $I = 11 - 23$ states in the [11,02] configuration of ^{64}Zn. The spherical origin of the orbitals is traced schematically, first by varying the deformation and then by adding a cranking frequency, ω. At $\omega = 0$, the orbitals are labelled by their oscillator shell, $\mathcal{N}$, and by the position in that $\mathcal{N}$-shell as a subscript. Symbols (circles and dots) are drawn at the frequencies corresponding to the $I = 11, 13, \ldots, 23$ states while the deformation at these angular momentum values can be read out in Fig. 8. The frequency of the terminating $I = 23$ state is not well-defined and was chosen to give smooth curves for the single-particle energies. The orbitals which are either occupied or empty in the [11,02] bands assigned to the observed band A are drawn by thick shaded lines. For these orbitals, the aligned angular momentum along the symmetry axis at termination ($\gamma = 60°$) is given on the right–hand side.

FIG. 10. Comparison between the observed bands A and B (upper panel) and the calculated configuration assigned to band A and possible configurations which could be assigned to band B. Experiment and theory has been normalized in the high-spin range of band A contrary to the more standard convention to normalize for the ground state. Aligned states at, or very close to, $\gamma = 60°$ are circled. Calculated energies of the [11,01] configuration are given both for the lowest minima and for the more collective minima where energy and deformation varies smoothly with angular momentum I.

FIG. 11. Neutron orbitals at a deformation close to that calculated for the yrast [11,02] configurations of ^{64}Zn at $I = 21, 22$. The parameters fitted to describe the positive parity states in ^{59}Cu are used [27]. The two orbitals which pass through a virtual crossing at $\omega \approx 0.12\omega_0$ are drawn with thick shaded lines.

Neutrons: $\varepsilon_2 = 0.268$, $\gamma = 33.4$, $\varepsilon_4 = 0.012$, $\kappa_n(3) = 0.095$, $\mu_n(3) = 0.29$